Derivatization and diffusive motion of molecular fullerenes: 
*Ab initio* and atomistic simulations

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Using first principles density functional theory in combination with the nonequilibrium Green’s function formalism, we study the effect of derivatization on the electronic and transport properties of C$_{60}$ fullerene. As a typical example, we consider [6,6]-phenyl-C$_{61}$-butyric acid methyl ester (PCBM), which forms one of the most efficient organic photovoltaic materials in combination with electron donating polymers. Extra peaks are observed in the density of states (DOS) due to the formation of new electronic states localized at/near the attached molecule. Despite such peculiar behavior in the DOS of an isolated molecule, derivatization does not have a pronounced effect on the electronic transport properties of the fullerene molecular junctions. Both C$_{60}$ and PCBM show the same response to finite voltage biasing with new features in the transmission spectrum due to voltage induced delocalization of some electronic states. We also study the diffusive motion of molecular fullerenes in ethanol solvent and inside poly(3-hexylthiophene) lamella using reactive molecular dynamics simulations. We found that the mobility of the fullerene reduces considerably due to derivatization; the diffusion coefficient of C$_{60}$ is an order of magnitude larger than the one for PCBM. © 2015 AIP Publishing LLC. [http://dx.doi.org/10.1063/1.4923352]

I. INTRODUCTION

Due to their prominent transport properties and electron accepting capability, fullerenes have a great potential for practical applications in organic electronics and photoochemistry.1–4 One of the notable applications of fullerenes is the fabrication of bulk heterojunction (BHJ) organic photovoltaic cells (OPVs), which consist of positive (p)-type conjugated polymers and n-type fullerene derivatives. The latter provides a promising framework, allowing the formation of a bicontinuous interpenetrating network of electron-donor and acceptor components within the active BHJ layer, which is a crucial factor for achieving high power conversion efficiency.5–7 Since such interpenetrating morphology controls many of the performance characteristics of bulk heterojunction organic photovoltaic cells,8–10 achieving the morphological stability, particularly under thermal stress conditions, is a key challenge to the commercialization of polymer-fullerene OPVs. One of the main reasons for the thermally induced degradation of solar cell performance is the diffusion of fullerene derivatives through the blend film.11–13 Although soluble fullerenes have major advances in a BHJ architecture, the thermal instability of BHJs, due partly to the diffusive motion of molecular fullerenes, must be addressed before one can consider them for practical applications in OPVs.14 Therefore, a fundamental understanding of the diffusive motion of fullerene derivatives within the blend under heat and light pressure is a key factor to increase the lifetime of OPVs.15 Here, we implement reactive molecular dynamics (MD) simulations to study the effect of derivatization of fullerenes on their diffusive motion in an ethanol. Derivatization is usually implemented to increase the solubility of fullerenes, thus allowing for solution processing and increase polymer compatibility and miscibility. As an example, we study the dynamics of the fullerene derivative PC$_{60}$BM ([6,6]-phenyl-C$_{61}$-butyric acid methyl ester), which is called PCBM in what follows, in ethanol solvent. We found that the derivatization reduces the mobility of the fullerene considerably inside the ethanol solvent; the diffusion coefficient is reduced by an order of magnitude due to the attached molecules. Diffusion of PCBM through and its intercalation within the donor polymer domain, formed poly(3-hexylthiophene) (P3HT) polymer is also studied. The mobility of PCBM is smaller as compared to the one for C$_{60}$ even in this environment. Note that the combination of electron-donating P3HT and electron-accepting PCBM forms one of the most efficient OPV materials.16–20

Because of the high electron mobility and affinity, fullerenes have attracted considerable attention as electron
acceptors and transport materials for organic electronic devices. Since pristine fullerenes are relatively insoluble, and therefore only amenable to thermal evaporation, derivatization is usually applied to increase their solubility. However, such functionalization is known to strongly affect the electronic and transport properties of low dimensional carbon based systems. Therefore, here we use first-principles Density Functional Theory (DFT) calculations in combination with the nonequilibrium Green’s function formalism to study the effect of derivatization on the electronic and transport properties of C\textsubscript{60} fullerene. As an example, we conduct simulations for a single PCBM molecule with pristine C\textsubscript{60} fullerene as a reference. We found that the functionalization has a considerable impact on the electronic properties of the fullerene. For example, extra peaks appear in the density of states (DOS) of the molecule due to the formation of new electronic states localized at/near the attached molecule. However, despite such peculiar features in the DOS of isolated molecules, derivatization does not have a pronounced effect on the electronic transport properties of fullerene molecular junctions, i.e., a fullerene attached to gold wires. Both systems show the same response to external voltage biasing: the transmission decreases with increasing applied voltage, except some resonance peaks in the transmission due to the voltage induced delocalization of some electronic states.

II. COMPUTATIONAL DETAILS

The structural and electronic properties of considered systems are studied using DFT calculations\textsuperscript{22} within the generalized gradient approximation (GGA) of Perdew-Burke-Ernzerhof (PBE) to represent the exchange-correlation energy.\textsuperscript{22} The samples were first geometry optimized using the convergence criteria for total energy of 10^{-4} eV and Hellman-Feynman forces less than 0.01 eV/Å. The electrostatic potentials were determined on a real-space grid with a mesh cutoff energy of 150 Ry and double-zeta-polarized basis sets. The eigenstates of the MPSH are associated with the Hilbert space spanned by the basis functions of the central atoms. The eigenstates of the MPSH are obtained by projecting the self-consistent Hamiltonian onto the Brillouin zone sampled with (4, 4, 100) points within the Monkhorst-Pack k-point sampling scheme. All the simulations are conducted using the first-principles computational package Atomistix toolkit (ATK).\textsuperscript{24}

In order to study the dynamical properties of fullerene derivatives in a solvent, we conducted MD simulations using reactive force-field ReaxFF, which is a general bond-order dependent potential that provides an accurate description of bond breaking and bond formation during chemical reactions.\textsuperscript{25} The connectivity in the entire system is recalculated in every iteration, enabling dissociation and formation of chemical bonds during the simulations. Non-bounded interactions (van der Waals and Coulomb) are calculated between all atom pairs, irrespective of connectivity, with a short range shielding term.\textsuperscript{25} Since ReaxFF parameters are derived from quantum chemical calculations, such force field gives energies, transition states, reaction pathways, and reactivity trends in agreement with quantum mechanical calculations and experiments.\textsuperscript{26–28} This approach has already been successfully used in describing carbon-based structures.\textsuperscript{29–31} MD simulations are conducted using the computational package LAMMPS.\textsuperscript{32,33}

III. ELECTRONIC TRANSPORT PROPERTIES OF C\textsubscript{60} AND PCBM

We start with considering the electronic properties of isolated C\textsubscript{60} and PCBM molecules by calculating the energy dependence of the electron DOS and their molecular energy spectrum. We first conducted structural optimization of both samples using the convergence criterium for energy as 10^{-4} eV between two consecutive steps, and for the maximum force on each atom less than 0.01 eV/Å. The main panel in Fig. 1 shows the DOS of C\textsubscript{60} (solid-black curve) and PCBM (dashed-red curve) molecules as a function of electron energy. The DOS of the pristine fullerene shows well separated peaks both above and below the Fermi level. Every maximum corresponds to a molecular energy state, as shown in panels 1 and 2 in Fig. 1, where we present the isosurface plots of the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO), respectively (the energies of the states are indicated by vertical-green lines in the main panel). Both HOMO and LUMO states are characterized by electronic states extended over the entire molecule. They are located at the same energy range away from the Fermi level and the HOMO-LUMO energy gap is 1.64 eV.

For the case of PCBM, when we attached the molecule it results in considerable changes in the DOS (dashed-red curve in the main panel of Ref. 1). First, the electron density decreases as compared to one of the pristine fullerenes (compare solid-black and dashed red curves). Second, the HOMO-LUMO gap becomes slightly smaller (1.47 eV). The most pronounced effect of fullerene derivatization is the presence of additional low amplitude peaks in the energy dependence of DOS. These peaks are due to the formation of electronic localized states at/near the attached molecule. Some examples of such delocalized states are shown in panels 5 and 6, where we plot the projected molecular self-consistent Hamiltonian (MPSH) eigenstates at energies indicated by O\textsubscript{1} and O\textsubscript{2} in the main panel. MPSHs are obtained by projecting the self-consistent Hamiltonian onto the Hilbert space spanned by the basis functions of the central atoms. The eigenstates of the MPSH are associated with the poles of the Green’s function and, in general, correspond approximately to the peaks in the transmission spectrum. Thus, the derivatization has a considerable effect on the DOS of fullerenes.

Next, we study the effect of fullerene derivatization on its electronic transport properties and take PCBM as an
example. For that purpose, we constructed a two probe devise geometry where the optimized PCBM is connected to gold wires through sulfur bonding [see Fig. 2(b)]. Gold-sulfur bonding plays an important role in such molecular junctions, resulting in enhanced stability of such nanostructures and increased electronic transmission between gold and sulfur-containing organic molecules (see Ref. 34 for review). The gold wires are consequently connected to metallic electrodes of size 7.064 Å.

As a main result, we present in Fig. 3 the zero bias transmission spectra (a), $T(E)$, and device density of states (DDOS) (b) as a function of the electronic energy for $C_{60}$ (solid-black curves) and PCBM (dashed-red curves). The energy origin is set to be the Fermi level of the system. For both samples, the transmission spectrum is characterized by well separated peaks with different amplitudes both below and above the Fermi level. The amplitude of the peaks is smaller near the Fermi level as compared to the amplitude of the resonance peaks away from the Fermi energy. These features are also reflected in the DDOS of the system as sharp peaks [see Fig. 3(b)], indicating that there is a correspondence between the energy levels of the samples and the transmission spectrum, this is in particular, through the location of their peaks.

At energies away from the Fermi level, the amplitudes of the transmission peaks are almost the same for both samples. However, near the Fermi energy some peaks become larger for PCBM, despite the similar density of states (see Fig. 3). To understand the origin for such local enhancement of the transmission in PCBM, we calculated and compared the transmission eigenstates for different transmission eigenstates at energies corresponding to the resonance peaks in the transmission spectrum. As an example, we show in panels 1 and 2 of Fig. 3 isosurface plots of the transmission eigenstates corresponding to the largest eigenvalue at $E = 0.54$ eV, also indicated on the $T(E)$ curves in Fig. 3(a). It is seen from these plots that the electronic states for $C_{60}$ are mostly localized near the left electrode with a little extension to the second half of the fullerene (panels 1). However, for the case of PCBM the eigenstates are homogeneous across the sample with larger electron density as compared to $C_{60}$.
Such delocalization of the states increases the probability of the electrons to cross the system. Thus, derivatization does not have a pronounced effect on the electronic transport in molecular junctions involving fullerenes, except for small features in the transmission spectrum near the Fermi level.

In what follows, we study the response of the considered samples to finite voltage biasing. As a typical example, we present in Fig. 4 the transmission spectra of both C$_{60}$ (a) and PCBM (b) for two values of the applied voltage: $V = 0.5$ V (dashed-red) and $V = 1$ V (dotted-blue) (the transmission spectra at zero voltage are presented as a reference by the solid-black curves). We show mostly the region near the Fermi level of the spectra, since for small bias this is the relevant energy range that contributes to carrier transport. It is seen from Fig. 4(a) that the electron transmission spectrum of C$_{60}$ changes slightly by applying a potential difference across the sample. For example, the transmission is reduced for most of the electron energies except some of the resonance peaks, where the transmission becomes larger at finite biasing. Energy dependent asymmetry in the transmission spectrum is preserved at finite voltage. The PCBM system also shows similar response to voltage biasing [Fig. 4(b)].

The most prominent feature of the voltage dependence of the transmission for both samples is the increase of the amplitude and broadening of some resonance peaks [see colored regions in Figs. 4(a) and 4(b)]. Calculations for the electron transmission eigenstates show that some states near the transmission peaks become more extended by applying an external voltage (see panels 1 and 2 in Fig. 4), which enhances the electronic transmission through the system. The amplitude of the peaks increases with further increasing the applied voltage, indicating the opening of extra transport channels for the electron. Thus, both considered systems show similar response to the applied voltage with new features in the transmission spectrum.

**IV. DYNAMICS OF C$_{60}$ AND PCBM**

In this section, we study the diffusive motion of C$_{60}$ and PCBM inside an ethanol solvent and P3HT lamella using classical MD simulations. Our choice of these solvents is based on the facts that ethanol is known as a good general purpose solvent and P3HT forms one of the promising BHJ OPVs in combination with PCBM. For our study, we used the ReaxFF force field developed by Monti et al. To validate this force field for our systems, we have optimized all...
considered structures using ReaxFF and compared them with the equilibrium structures obtained using DFT/PBE. As an example, we plot in Fig. 5 the optimized structures of PCBM (a) and (b) and P3HT (c) and (d) obtained using DFT/PBE (a) and (c) and ReaxFF (b) and (d). Bond distances between selected atoms are shown for comparison.

![Optimized structures](image)

FIG. 5. Optimized structures: equilibrium structures of PCBM (a) and (b) and P3HT (c) and (d) optimized using DFT/PBE (a) and (c) and ReaxFF (b) and (d). Bond distances between selected atoms are shown for comparison.

We first consider the dynamics of PCBM inside the ethanol solvent. Dynamics of pristine fullerene C_{60} is also studied for the same conditions as reference. As a main result, we present in Fig. 6(a) the mean square displacement \langle R^2 \rangle of the C_{60} (solid-black curve) and PCBM (dashed-red curve) at temperatures $T = 300$ K as a function of time, where $R^2 = x^2 + y^2 + z^2$. Since the deformation of fullerene is small at these low temperatures, we used the transverse motion of the center of mass of the fullerene ball in constructing the \langle R^2 \rangle(t) curves of both systems. It is seen from this figure that the difference in \langle R^2 \rangle becomes significant already at small times: the distance that C_{60} travels in ethanol solvent becomes an order of magnitude larger than the one that is covered by PCBM. This is also clearly seen from Figs. 6(b) and 6(c), where we plot the trajectories of C_{60} (a) and PCBM (b) during the time of a simulation 500 ps at 300 K. Diffusion coefficients are obtained from the mean square displacement in the large time region [see the yellow region in Fig. 6(a)] as $D = 0.166$ Å²/ps and $D = 0.034$ Å²/ps for C_{60} and PCBM, respectively. The found 5 fold decrease of the diffusion coefficient indicates the significance of the derivatization of fullerenes for performance and durability of OPVs.

As we mentioned above, the interpenetrating morphology formed by the electron donor and acceptor materials is critical for the performance of polymer-fullerene BHJ photovoltaic (PV) cells. This also necessitates fullerene derivatization to increase its solubility which is needed to obtain the desired morphology and stability of the active layer. In what follows, we study the dynamics of PCBM and C_{60} molecules inside P3HT-lamellae, which is considered as one of the promising electron donating polymers in organic solar cell materials. To quantify the mobility of the considered molecules, we show in Fig. 7(a) the mean square displacement \langle R^2 \rangle of C_{60} (solid-black curve) and PCBM (dashed red curve) at $T = 300$ K. At small times (t ≤ 100 fs), both molecules show the same time dependence of \langle R^2 \rangle. With increasing time, there is a deviation of the curves and the mobility of C_{60} becomes significantly larger at larger times. The diffusion coefficients of C_{60} and PCBM are $D = 0.018$ Å²/ps and $D = 0.001$ Å²/ps, respectively, indicating that fullerene...
derivation has a considerable effect on the diffusive motion of fullerenes in different solvents. For example, derivatization can result in a reduction of the diffusion coefficient of fullerenes by an order of magnitude. Our findings can be useful in the understanding of the evolution of the BHJ morphology during the thermal annealing, as well as in understanding the relationship between the morphology of the phase-separated polymer/fullerene blends and the photophysics of the excited states involved in the charge transfer process.

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V. CONCLUSIONS

First-principles DFT calculations in combination with the Green’s functional formalism were used to study the effect of functionalization on the electronic and transport properties of fullerenes. Simulations are conducted for pristine C60 molecule and for its derivative PCBM, which is known to be one of the promising organic compounds to be used in OPVs. Although PCBM shows a richer density of states due to the localized states near/at the attached molecule, similar electronic transport properties have been obtained for the molecular junction made of this molecule as compared to the device made of pristine fullerene. In addition, both systems show similar response to an applied potential difference with new features in the transmission spectrum. However, as our MD simulations revealed, functionalization indeed reduces the mobility of fullerenes. Note that the smaller diffusion constants of the fullerenes (fullerene derivatives) inside P3HT as compared to the ones inside ethanol are due to the larger density of molecules in the former case. Figures 7(b) and 7(b) show the trajectories of C60 and PCBM, respectively, which clearly show the larger diffusion area of the C60 molecule as compared to PCBM. For this solvent, C60 molecule performs mostly circular motion, whereas PCBM does not show such a behavior. The other non-circular trajectories are also obtained during the statistical calculations. Note that the interaction between the molecules and the solvents is purely non-bounded (van der Waals and Coulomb) at the considered temperature. Thus, derivatization considerably reduces the mobility of the fullerenes in the different solvents.

FIG. 7. (a) Mean-square displacement $\langle R^2 \rangle$ ($\text{Å}^2$) as a function of time for the motion of the C60 (solid-black curve) and PCBM (dashed-red curve) molecules at $T = 300$ K inside P3HT lamella in a simulation box of $50 \times 50$ Å $\times 50$ Å with periodic boundary conditions in all directions. The region that is used to estimate the diffusion coefficient is highlighted by the yellow area. (b) and (c) $x$-$y$-trajectories of C60 (b) and PCBM (c).